

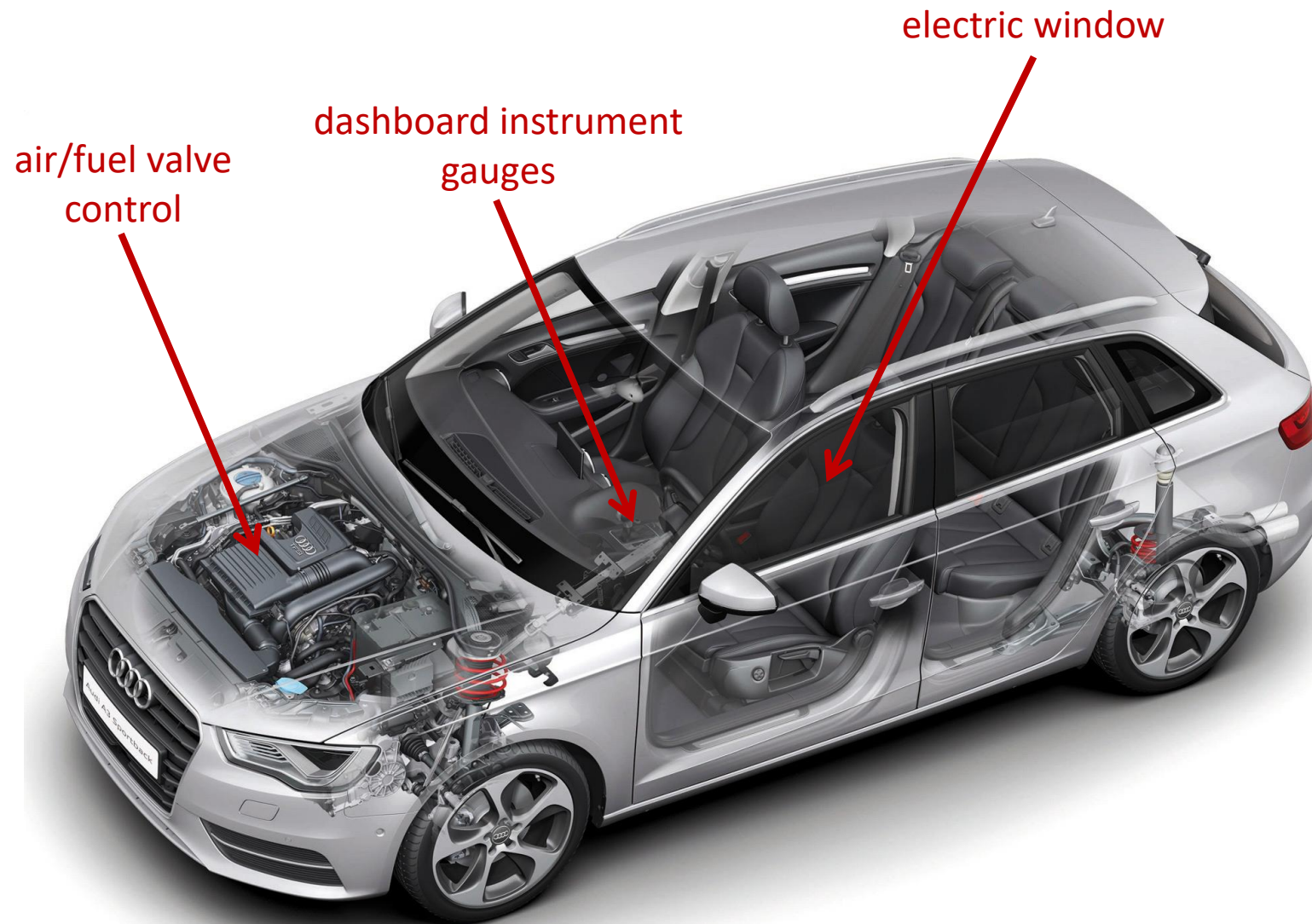


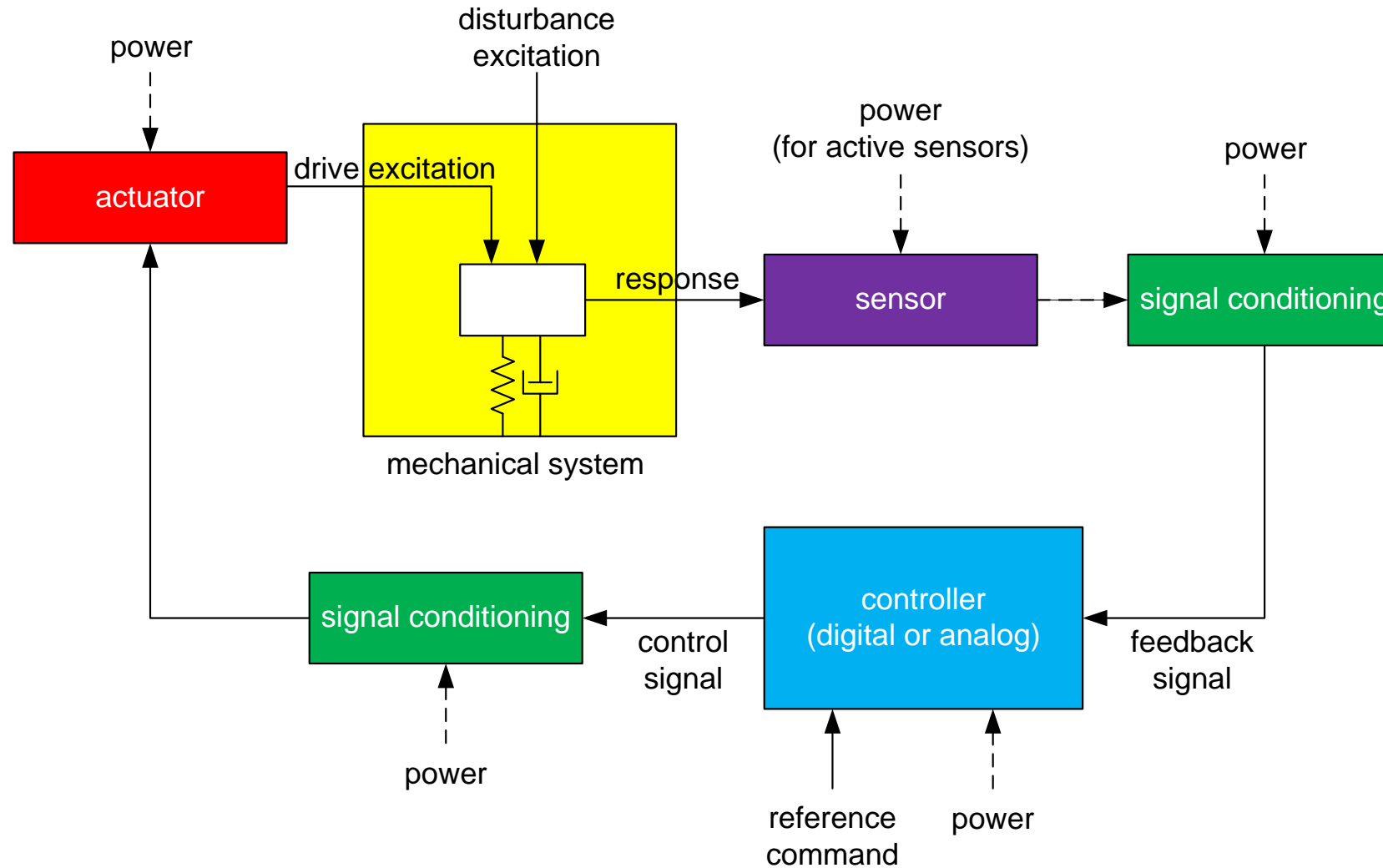
Sensing, Computing, Actuating

Sander Stuijk (s.stuijk@tue.nl)

STEPPER MOTOR

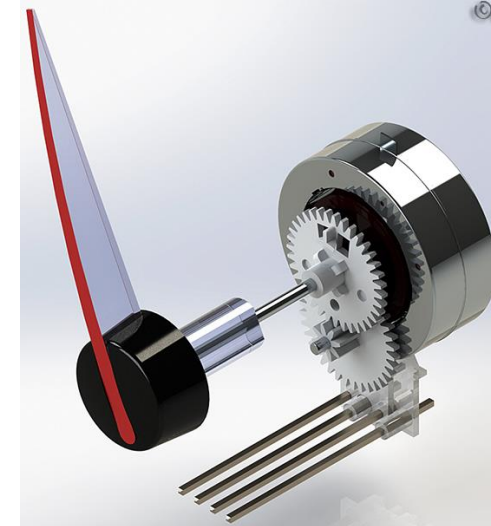
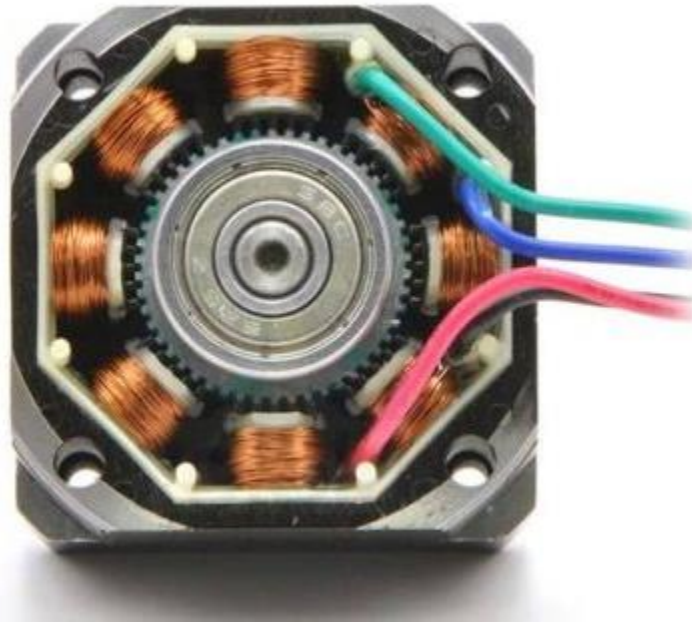
(Chapter 8.1, 8.2, 8.7, 8.8)



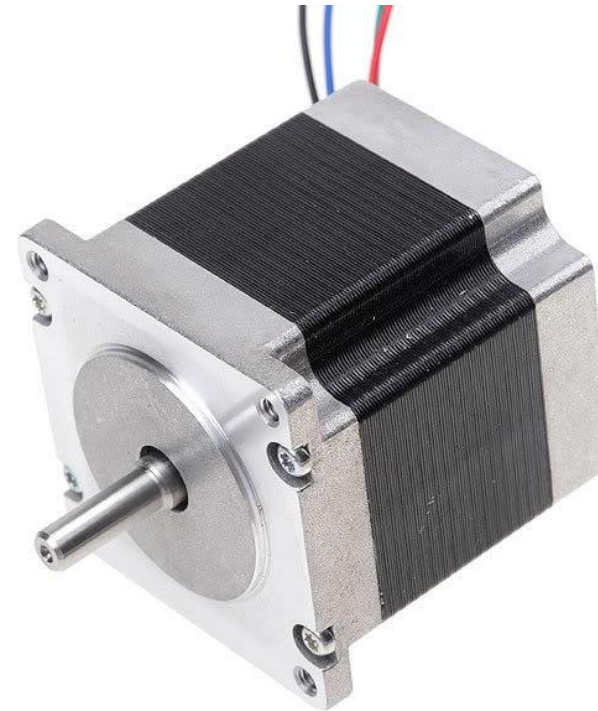
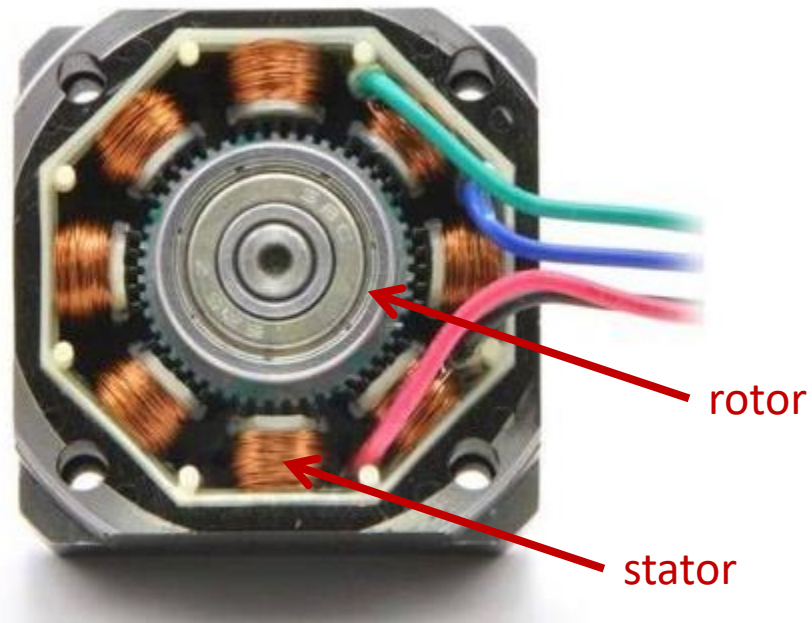


Stepper motor

- converts **digital** electrical signal to mechanical signal
 - fixed angular step per pulse
 - typical values: 2°, 2.5°, 5°, 7.5°, 15°
 - available in several horse power ratings
 - can track input signal up-to 1200 pulses/sec.

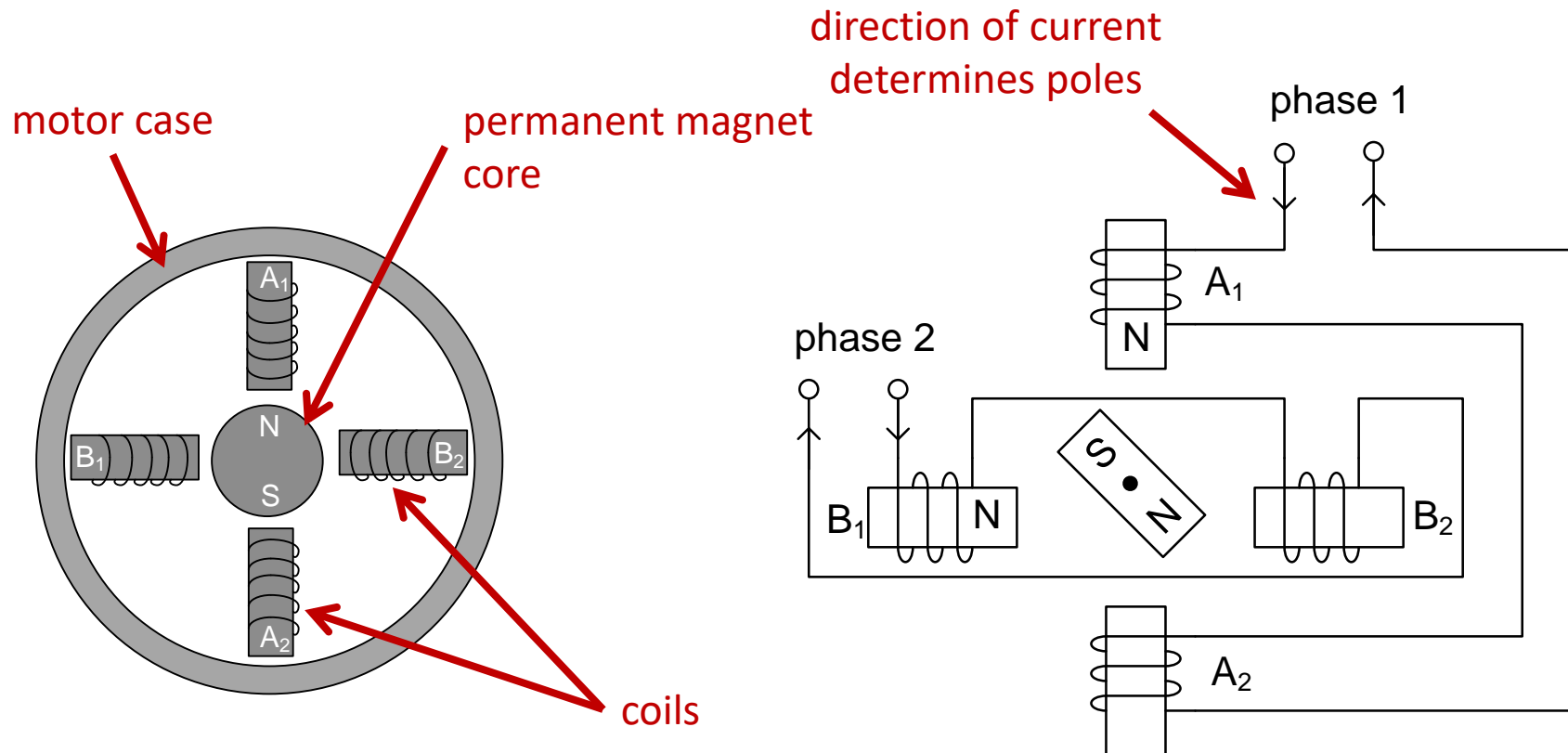


- 3 types of stepper motors
 - variable-reluctance (VR) with soft-iron core (teeth on rotor)
 - permanent-magnet (PM) with magnetized rotors
 - hybrid (HB) combination of VR and PM

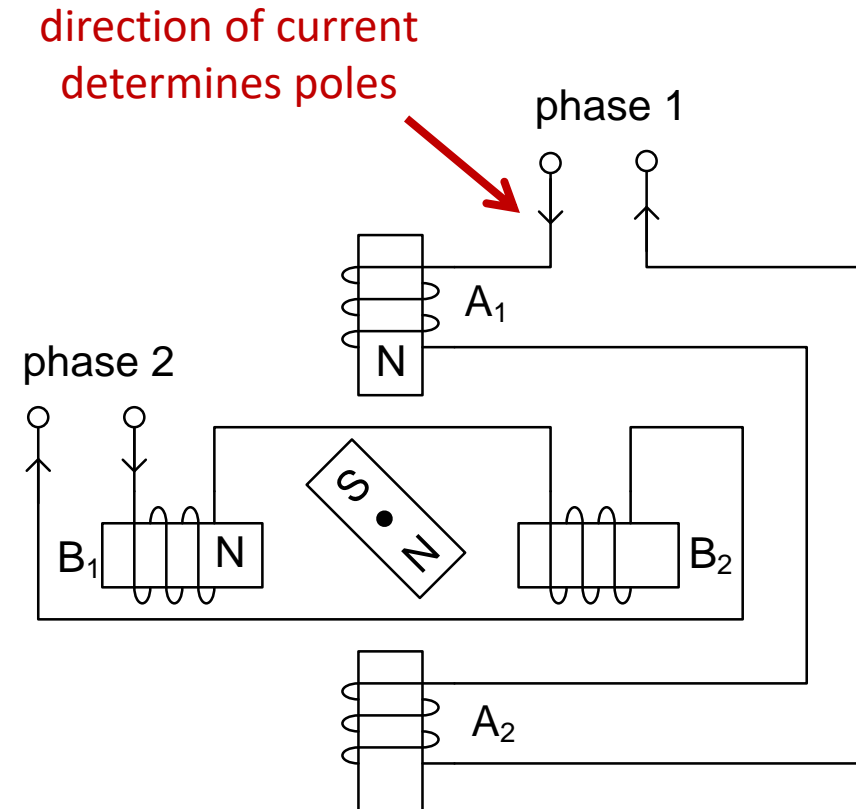
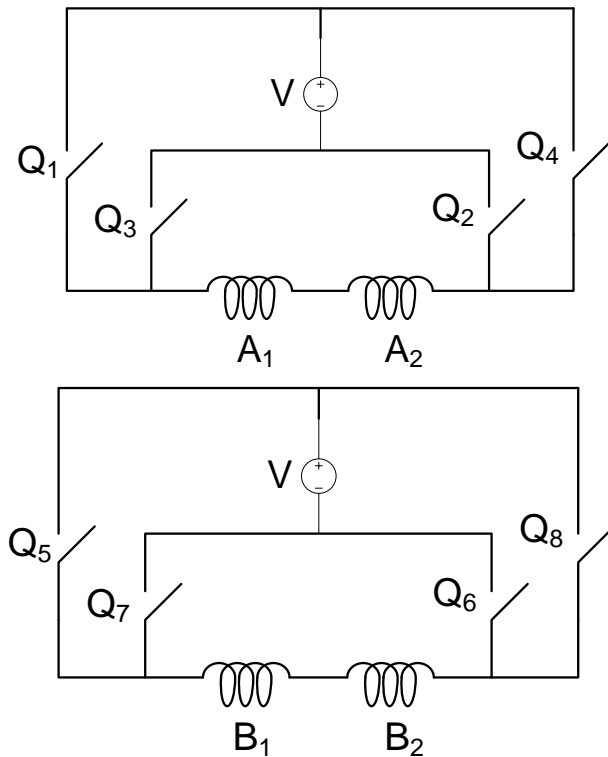


Permanent magnet step motor

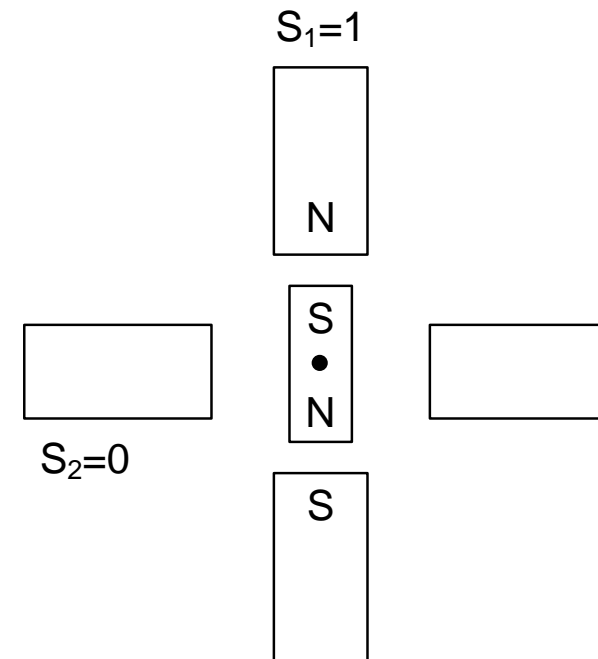
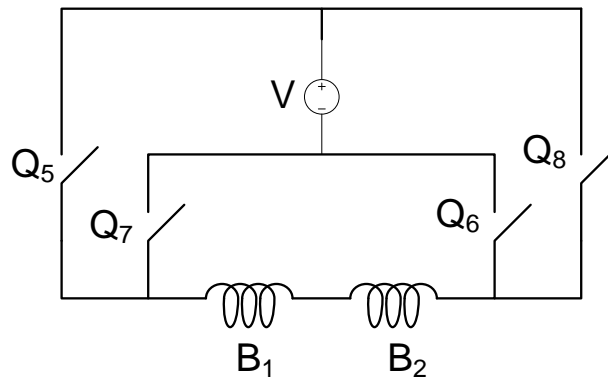
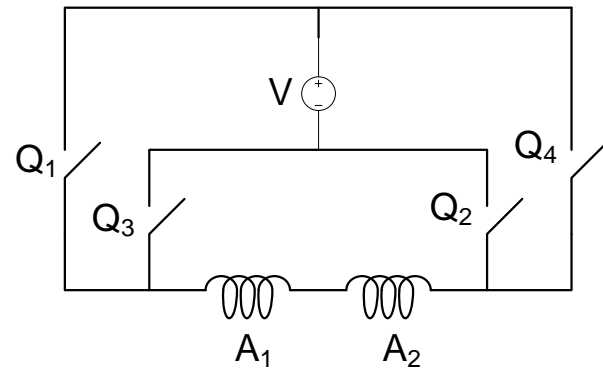
- two-phase two-pole permanent magnet step motor
 - two phases → two windings
 - two-poles → rotor has one permanent magnet



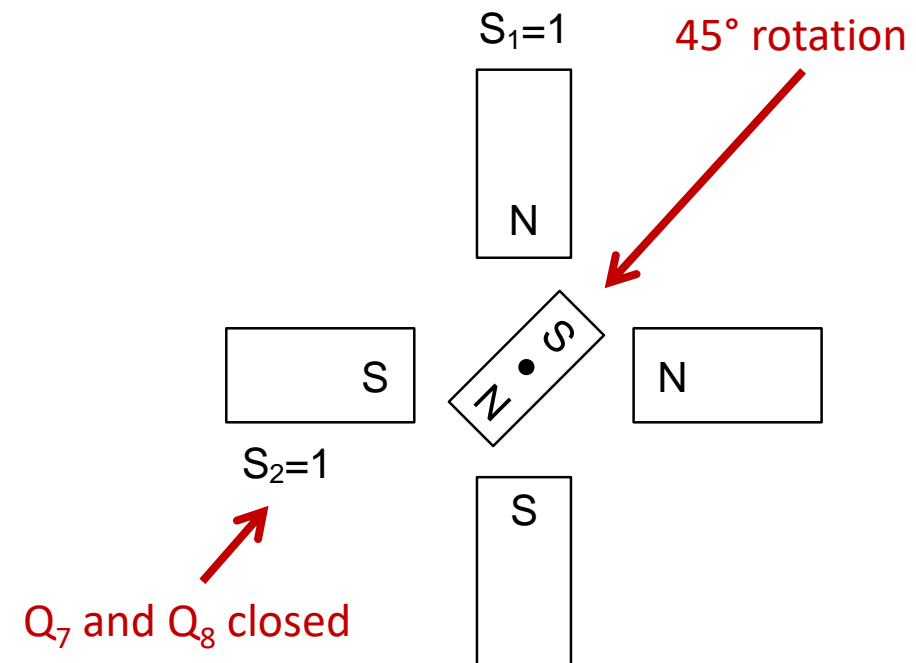
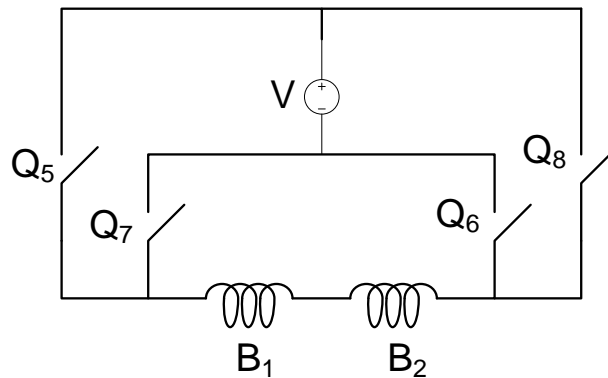
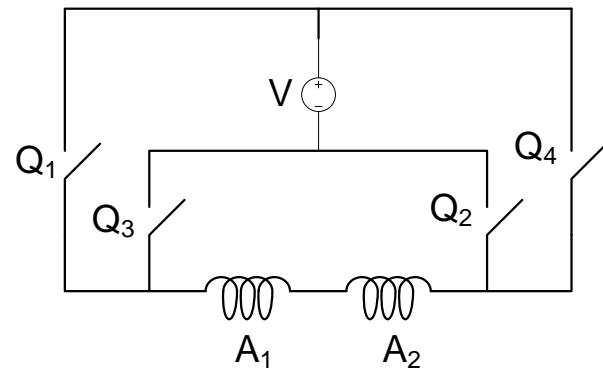
- dc voltage applied to both phases
 - direction of current through windings A1 and A2 controlled with switches Q1, Q2, Q3, Q4
 - direction of current through windings B1 and B2 controlled with switches Q5, Q6, Q7, Q8



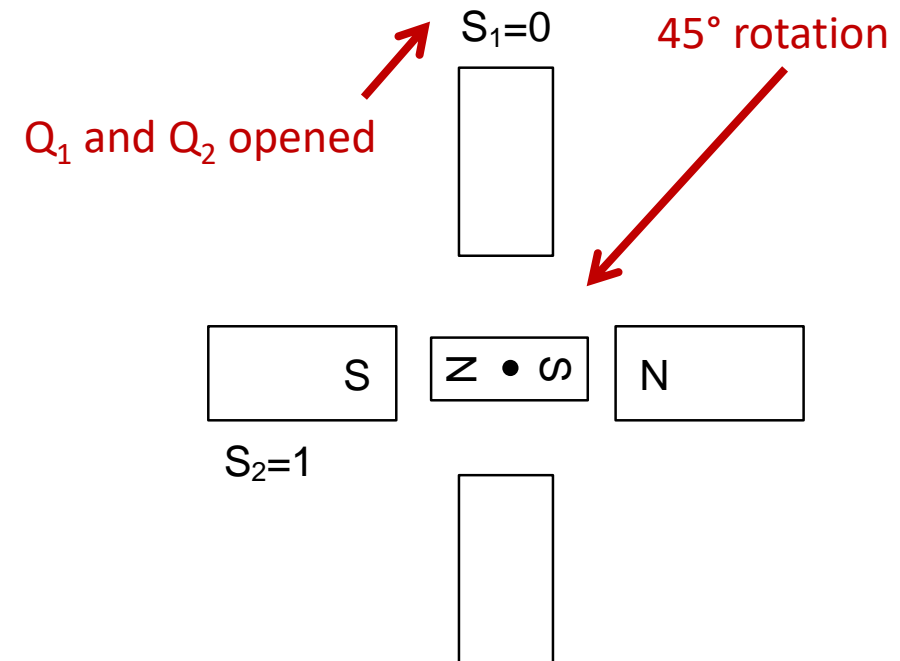
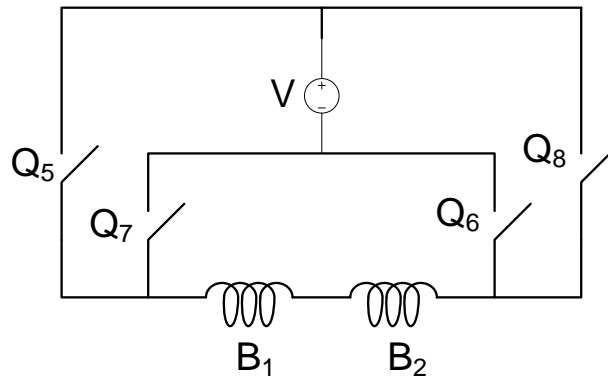
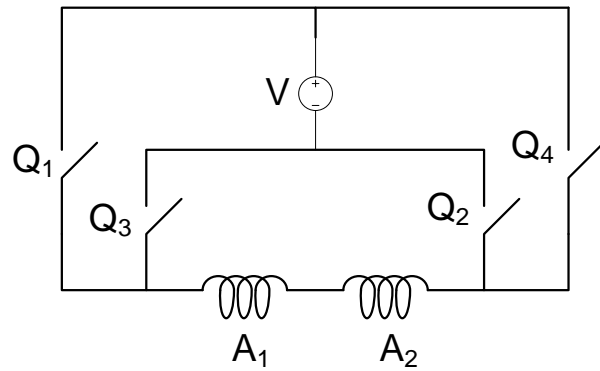
| | step 1 | step 2 | step 3 | step 4 |
|-----------|----------------|--------|--------|--------|
| Q_1-Q_2 | ON ($S_1=1$) | | | |
| Q_3-Q_4 | | | | |
| Q_5-Q_6 | | | | |
| Q_7-Q_8 | | | | |



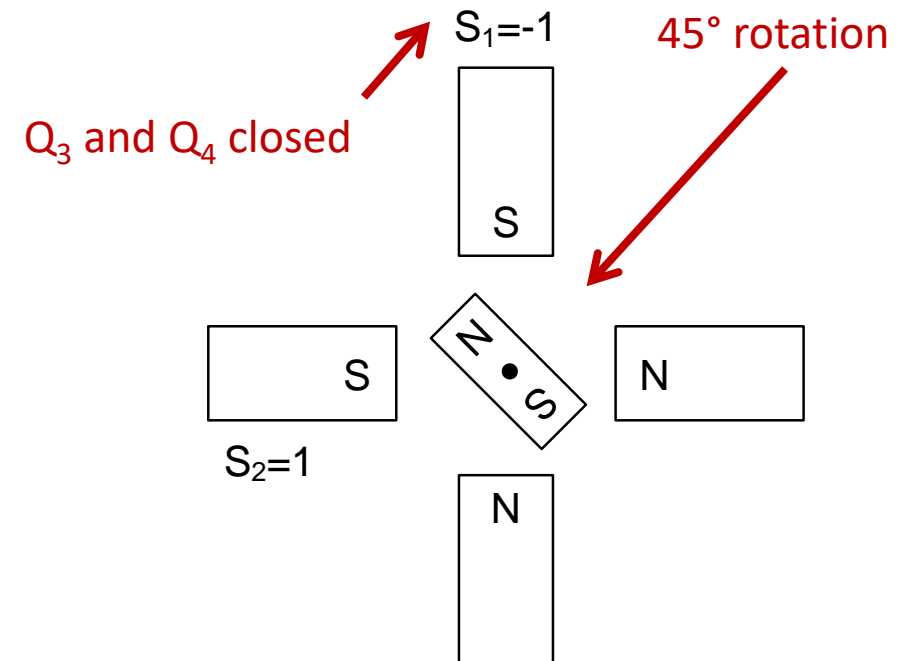
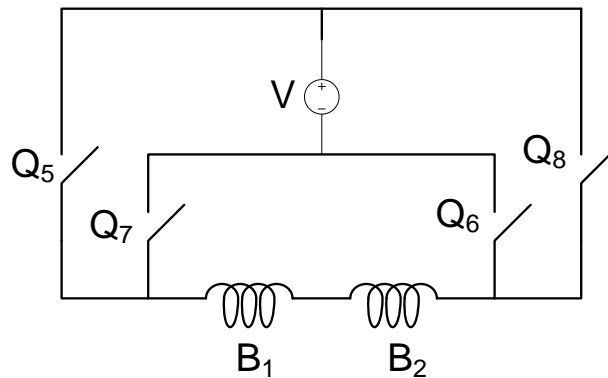
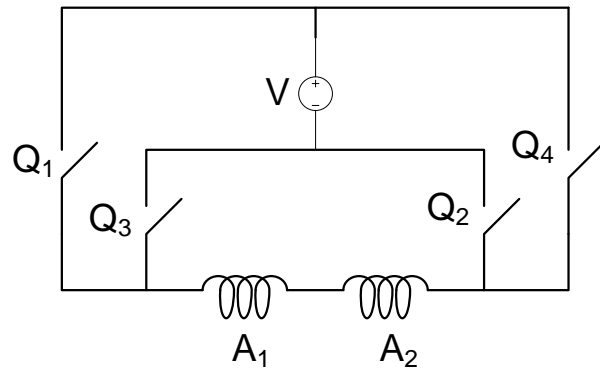
| | step 1 | step 2 | step 3 | step 4 |
|--------------------------------|------------------------|------------------------|--------|--------|
| Q ₁ -Q ₂ | ON (S ₁ =1) | ON (S ₁ =1) | | |
| Q ₃ -Q ₄ | | | | |
| Q ₅ -Q ₆ | | | | |
| Q ₇ -Q ₈ | | ON (S ₂ =1) | | |



| | step 1 | step 2 | step 3 | step 4 |
|--------------------------------|------------------------|------------------------|------------------------|--------|
| Q ₁ -Q ₂ | ON (S ₁ =1) | ON (S ₁ =1) | | |
| Q ₃ -Q ₄ | | | | |
| Q ₅ -Q ₆ | | | | |
| Q ₇ -Q ₈ | | ON (S ₂ =1) | ON (S ₂ =1) | |



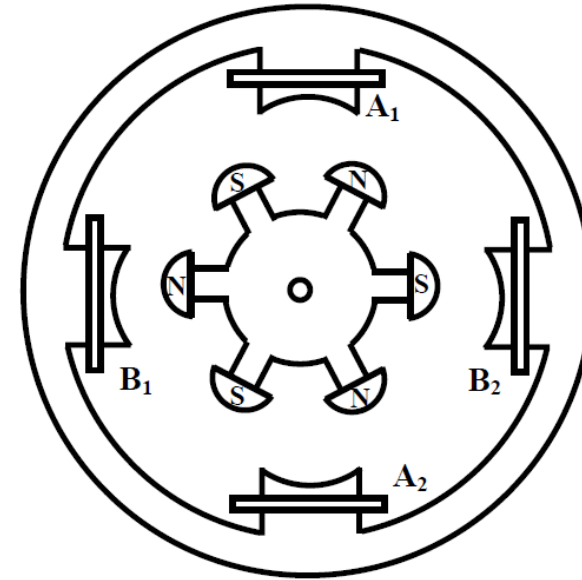
| | step 1 | step 2 | step 3 | step 4 |
|--------------------------------|----------------|----------------|----------------|-----------------|
| Q ₁ -Q ₂ | ON ($S_1=1$) | ON ($S_1=1$) | | |
| Q ₃ -Q ₄ | | | | ON ($S_1=-1$) |
| Q ₅ -Q ₆ | | | | |
| Q ₇ -Q ₈ | | ON ($S_2=1$) | ON ($S_2=1$) | ON ($S_2=1$) |



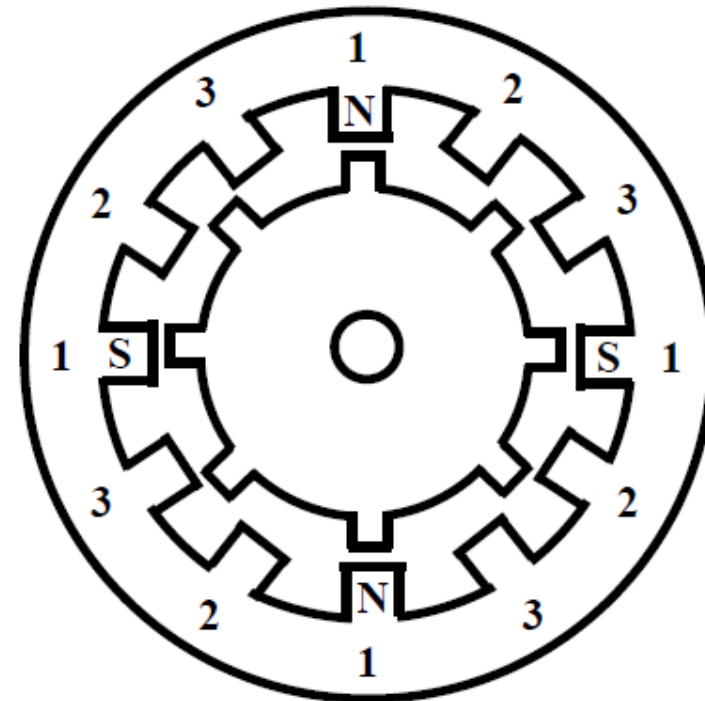
| | step 1 | step 2 | step 3 | step 4 |
|-----------|----------------|----------------|----------------|-----------------|
| Q_1-Q_2 | ON ($S_1=1$) | ON ($S_1=1$) | | |
| Q_3-Q_4 | | | | ON ($S_1=-1$) |
| Q_5-Q_6 | | | | |
| Q_7-Q_8 | | ON ($S_2=1$) | ON ($S_2=1$) | ON ($S_2=1$) |

- switching step angle 45°
- 8 steps needed for complete revolution
- each alternating step two windings are energized (**half stepping**)
- direction of **rotation reversed** by reversing step switching sequence

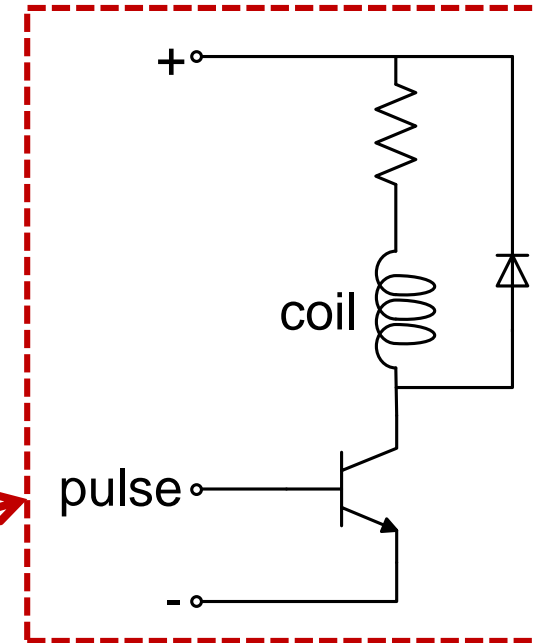
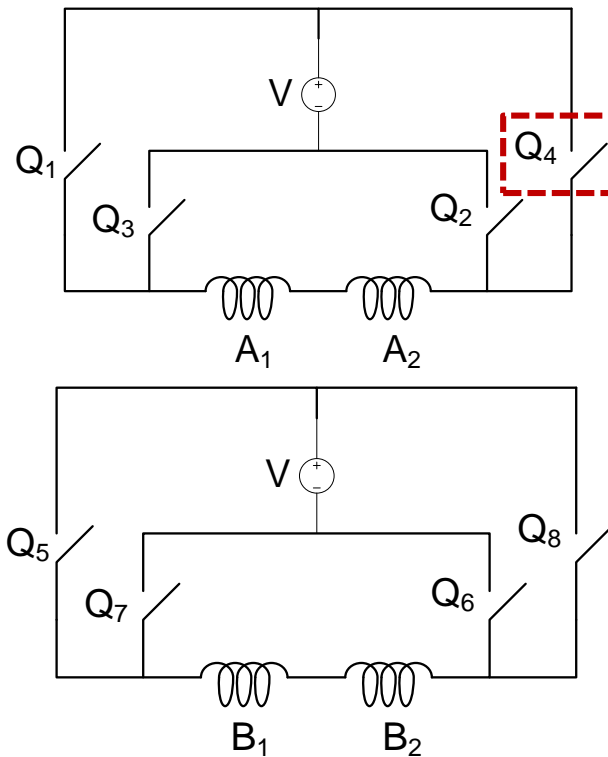
- example: two-phase six-pole permanent magnet motor
 - stator pitch $\Theta_s = 360^\circ / 4 = 90^\circ$
 - rotor pitch $\Theta_r = 360^\circ / 6 = 60^\circ$
 - full step angle $\Theta_{fs} = \Theta_s - \Theta_r = 30^\circ$
 - half step angle $\Theta_{hs} = (\Theta_s - \Theta_r) / 2 = 15^\circ$
- permanent magnet provides holding torque
 - rotor locks itself when coils are not energized
- direction of current needs to be reversed for each winding
 - requires transistor circuit
 - two solutions to this problem
 - use two windings per pole (one for each direction)
 - use variable magnet step motor



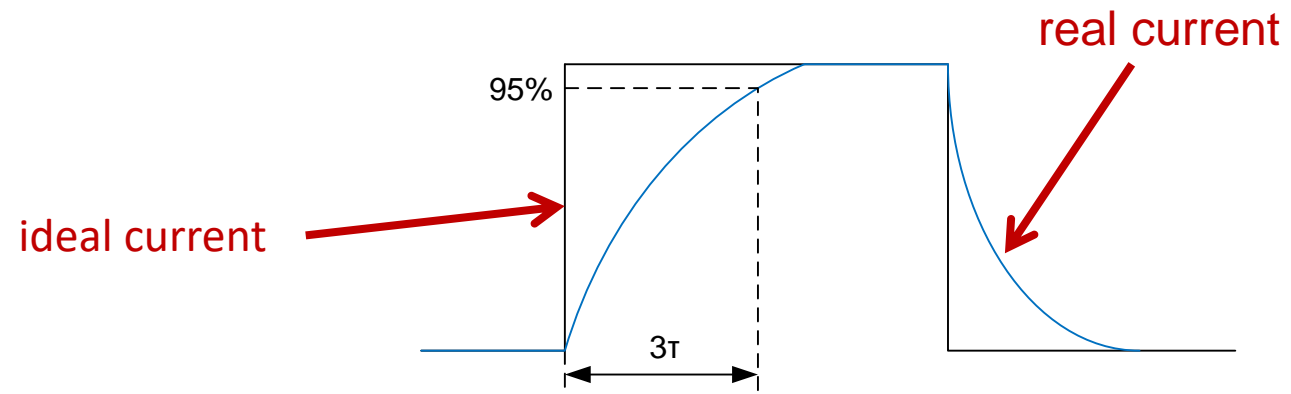
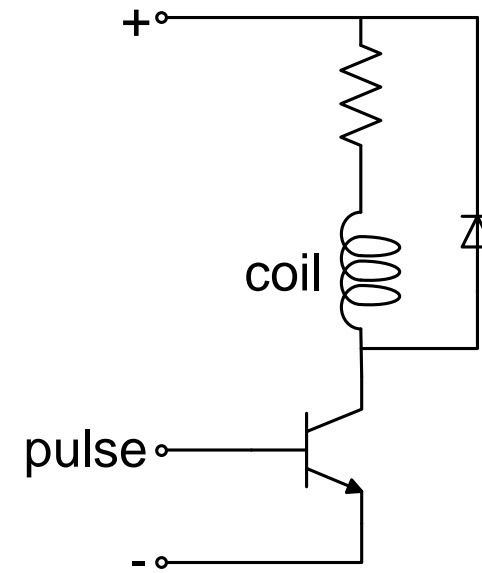
- cylindrical soft-iron core with projected teeth
- operation
 - energy specific stator coil (phase)
 - rotor aligns to minimum reluctance path
- example: three-phase, 12 stator teeth, 8 rotor teeth VR step motor
 - stator pitch $\Theta_s = 360^\circ / 12 = 30^\circ$
 - rotor pitch $\Theta_r = 360^\circ / 8 = 45^\circ$
 - full step angle $\Theta_{fs} = 15^\circ$
 - half step angle $\Theta_{hs} = 7.5^\circ$
- half-step counter clock-wise step sequence
1-(1,2)-2-(2,3)-3-(3,1)-1



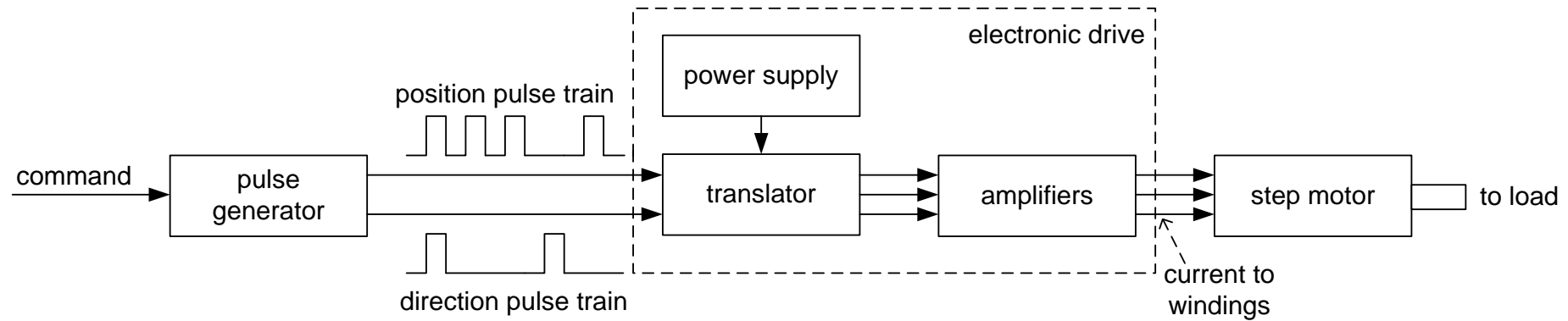
- switching transistor
 - positive voltage on base energizes coil
 - electromotive force is induced when current through coil stops
 - diode provides return path for current



- switching transistor
 - positive voltage on base energizes coil
 - emf is induced when current through coil stops
 - diode provides return path for current
- current pulse
 - presence of inductor causes delay in actual response
 - sufficient torque provided after 3τ (time constant)
 - pulse width should be $6-8\tau$

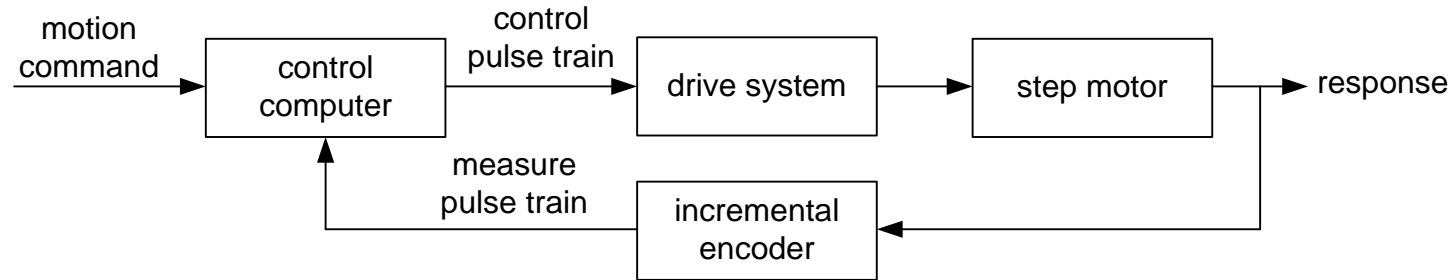


- open-loop control of step motor



- translator distributes position pulse train to phases
- direction of rotation reversed with direction pulses
- missed pulse may cause erratic behavior of rotor

- closed-loop feedback control of step motor

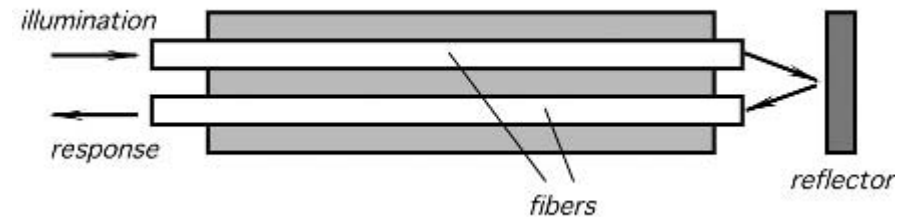


- sensor needed to measure rotation
- incremental optical encoder often used for this purpose

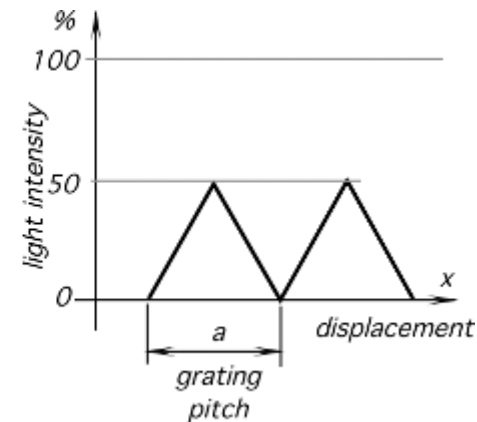
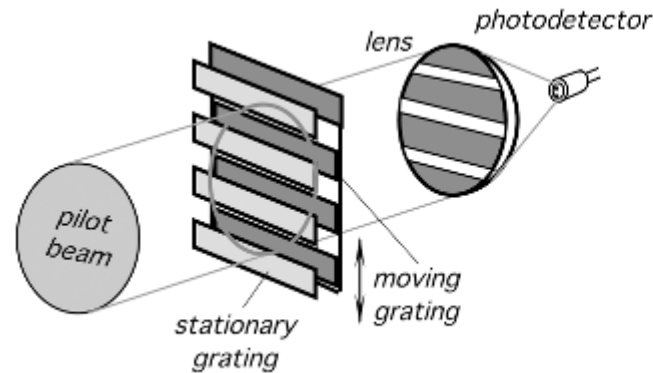
DIGITAL TRANSDUCERS

(Chapter 5)

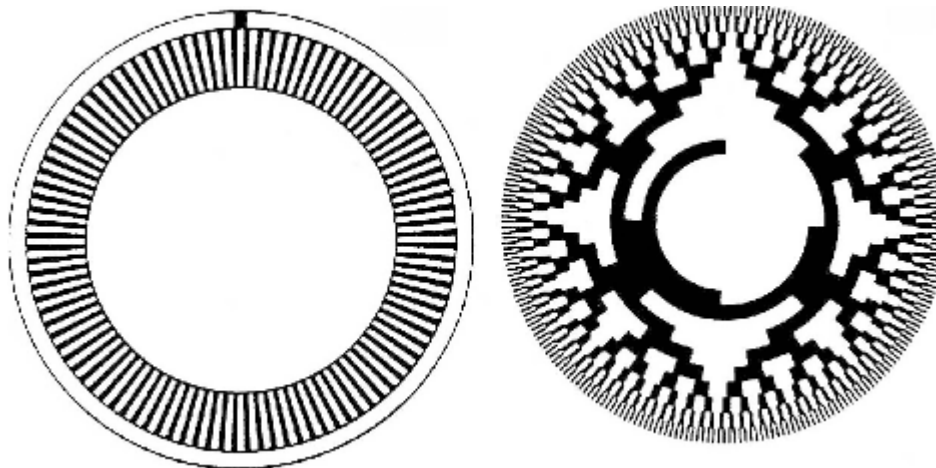
- optical sensors are widely used for position and displacement sensing
- advantages
 - no loading effects
 - relative long operating distances
 - insensitive to magnetic fields and electrostatic interference
- optical sensor consists of
 - light source
 - photo detector
 - light guidance device



- grating sensor is an optical displacement transducer
- two overlapping gratings serve as a light-intensity modulator
- operation
 - incoming light beam strikes first grating
 - grating passes 50% of light towards second, moving grating
 - depending on the alignment between the grating a fraction of the light can pass through this second grating
 - intensity of passed light is sensed with photo-detector

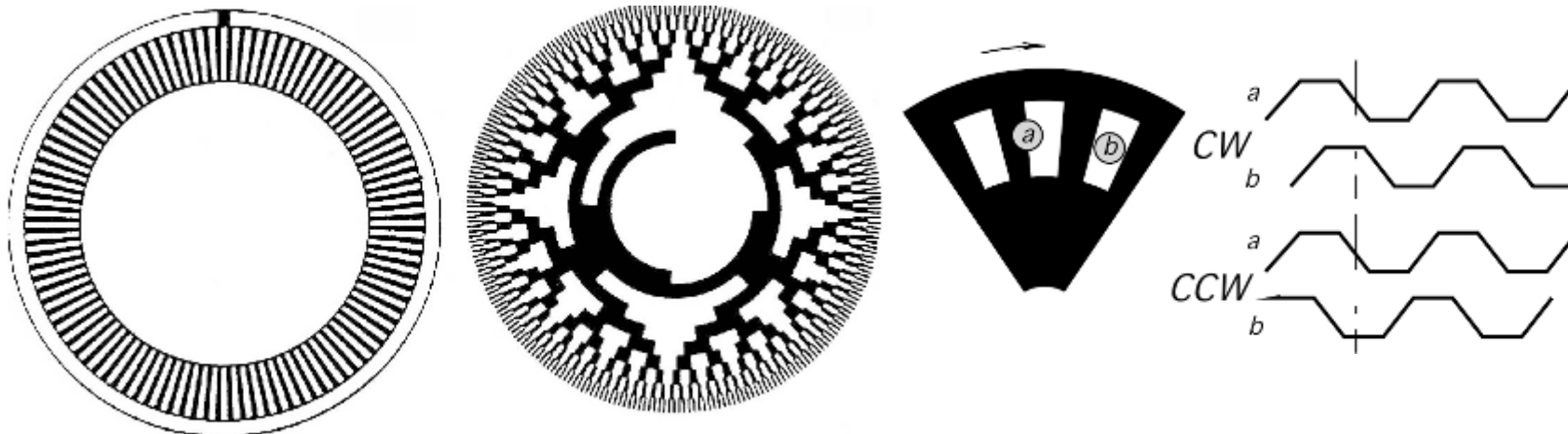


- full-scale displacement is equal to size of an clear (opaque) sector
- gives trade-off between sensitivity and dynamic range
 - large sensitivity requires small opaque sector (pitch)
 - large dynamic range (displacement) requires large pitch
- grating principle is used in rotating and linear encoders
- two types of encoders are distinguished
 - incremental position encoders (left)
 - absolute position encoders (right)

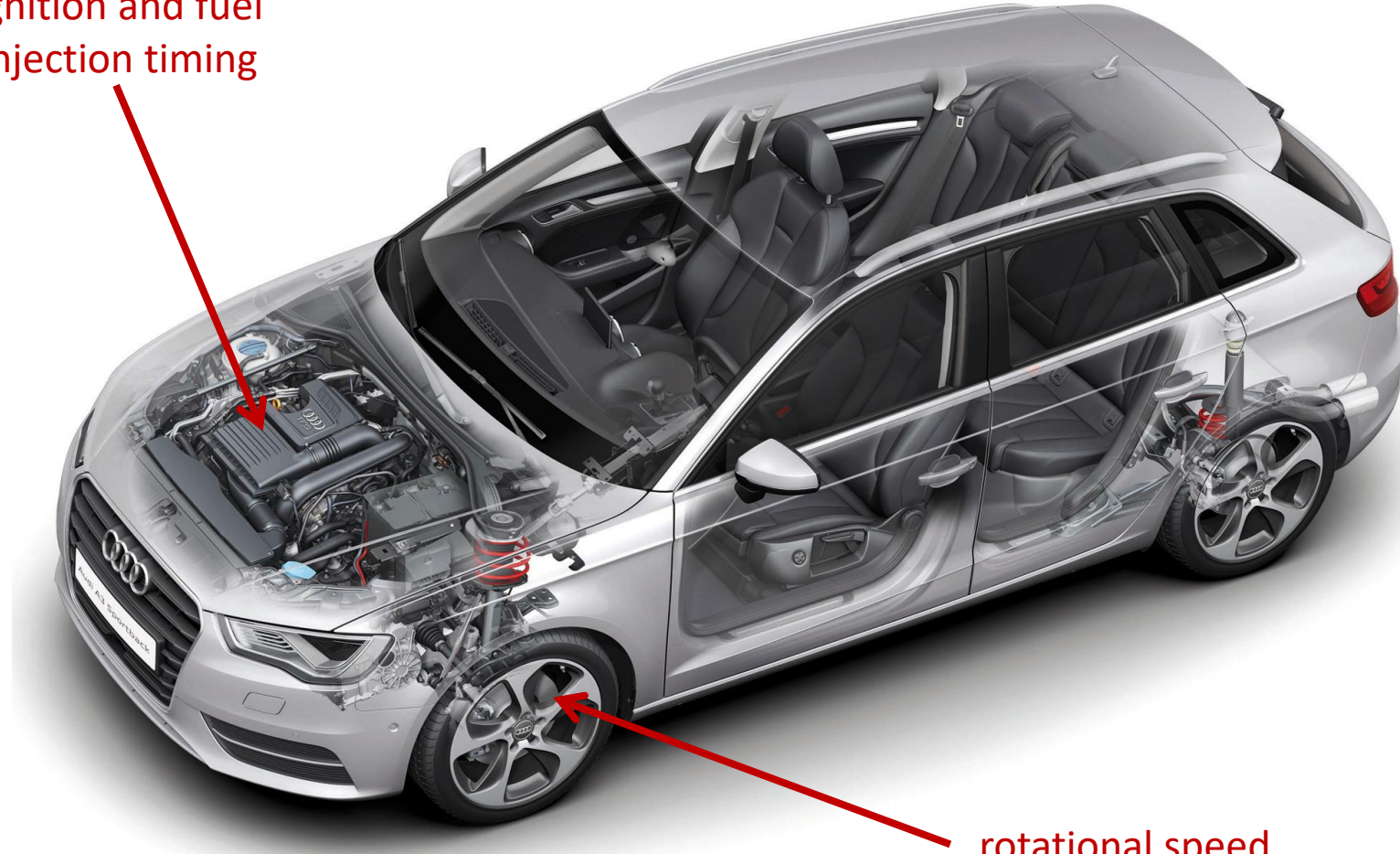


- incremental encoders produce a pulse when rotated for one pitch
- absolute encoders produce a binary value encoding position

- incremental encoders can use one or two optical channels
 - one channel allows sensing of movement
 - two channels allows sensing of movement and direction
 - use time difference between detectors a and b to determine direction (CW – clock-wise or CCW – counter-clock-wise)



ignition and fuel
injection timing

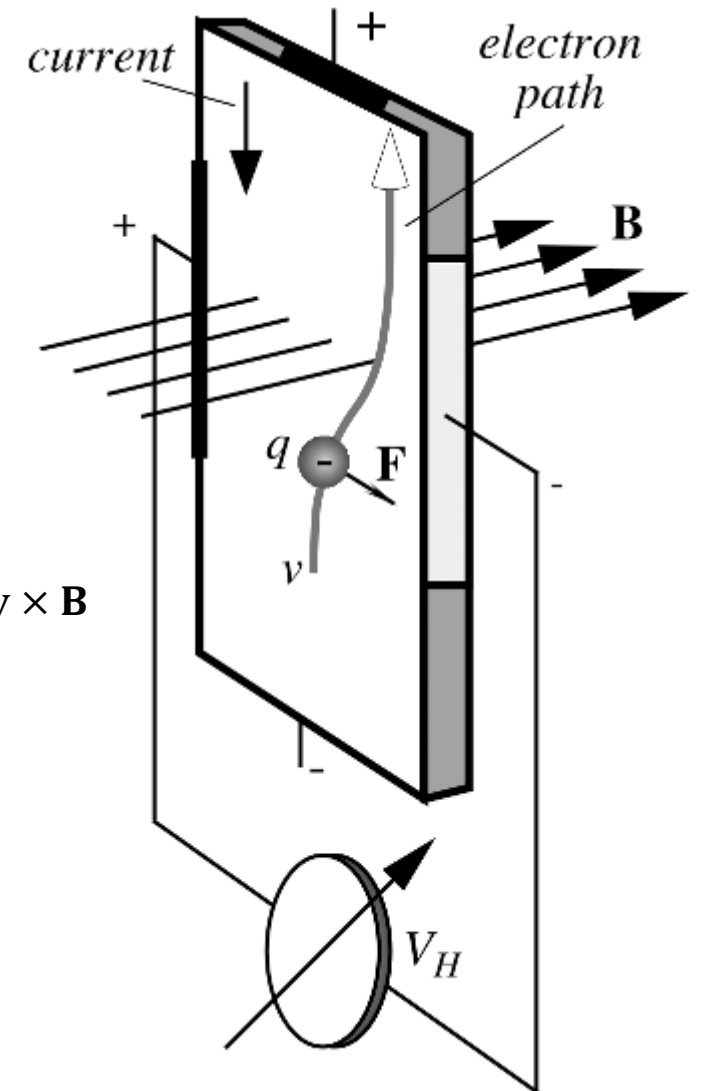


rotational speed

- effect discovered in 1879 by Edward Hall
- effect exists in all conducting materials
- used extensively in sensing position, displacement, and magnetic fields

- effect based on interaction between
 - moving electric carriers (i.e., electrons in metals or holes in semiconductors)
 - external magnetic field

- electron moving through magnetic field is subject to sideways Lorentz force $\mathbf{F} = q\mathbf{v} \times \mathbf{B}$
 - q – electronic charge ($1.6 \times 10^{-19} \text{C}$)
 - B – magnetic field
 - v – speed of an electron ($v = \mu EL$)
 - μ – carrier mobility
 - EL – longitudinal electrical field

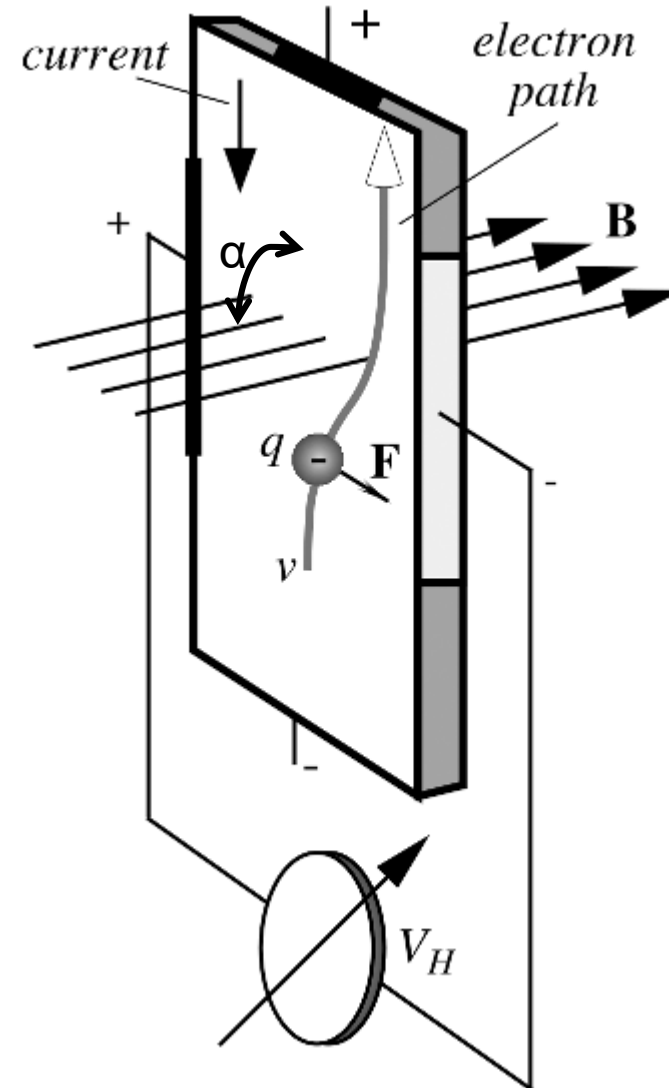


- Lorentz force causes charge carriers to accumulate on one side
 - electrons in conductors to right
 - holes in semiconductor to left
- force results in a transversal electrical field
- electrical field balances force exerted by magnetic field

- transverse Hall potential

$$V_H = \frac{1}{Nc} \frac{iB}{qd} \sin \alpha$$

- i – primary current
- N – free electrons per unit volume
- c – speed of light
- d – thickness of the conductive strip
- α – angle between magnetic field and strip



- transverse Hall potential

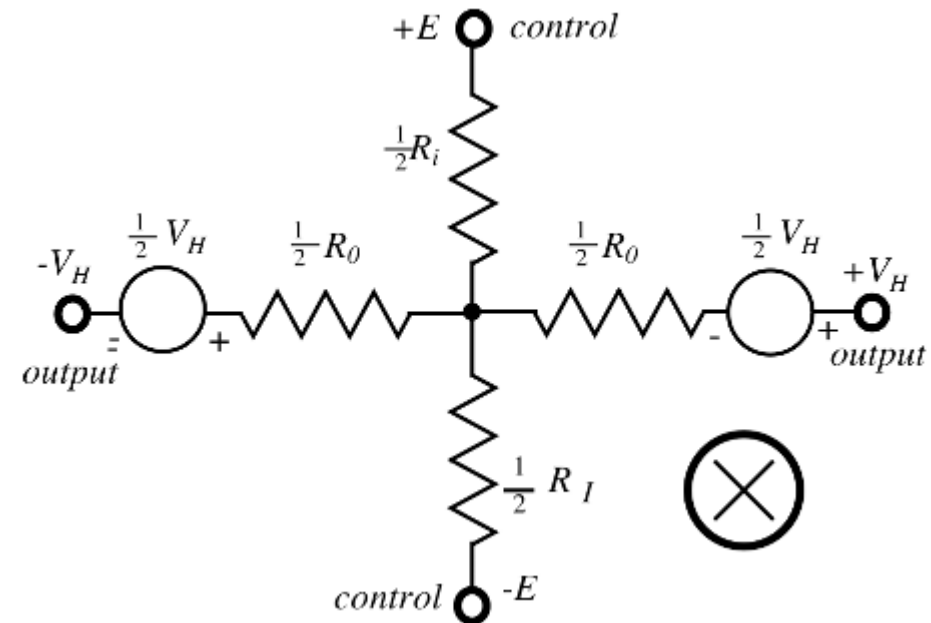
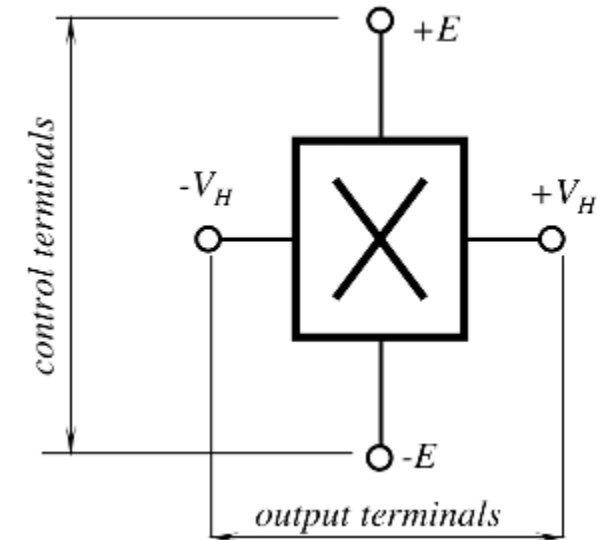
$$V_H = \frac{1}{Ncq} \frac{iB}{d} \sin \alpha$$

- factor $1/Ncq$ is material dependent and is called **Hall coefficient**
- polarity of V_H depends on **direction** of current and magnetic field
- **magnitude** of V_H depends on magnetic field strength (linear) and angle (non-linear)

- **how to use device as sensor?**
 - move magnetic object to/from sensor device (change **B**)
 - rotate magnetic object at fixed distance (change **α**)

- sensor packaged in four terminal housing
 - two control terminals
 - two output terminals
 - cross indicates direction of magnetic field
 - field moves away from viewer

- equivalent model for sensor
 - two control resistances R_i
 - two output resistances R_o
 - Hall effect voltage V_H



- characteristics of a semiconductor Hall effect sensor

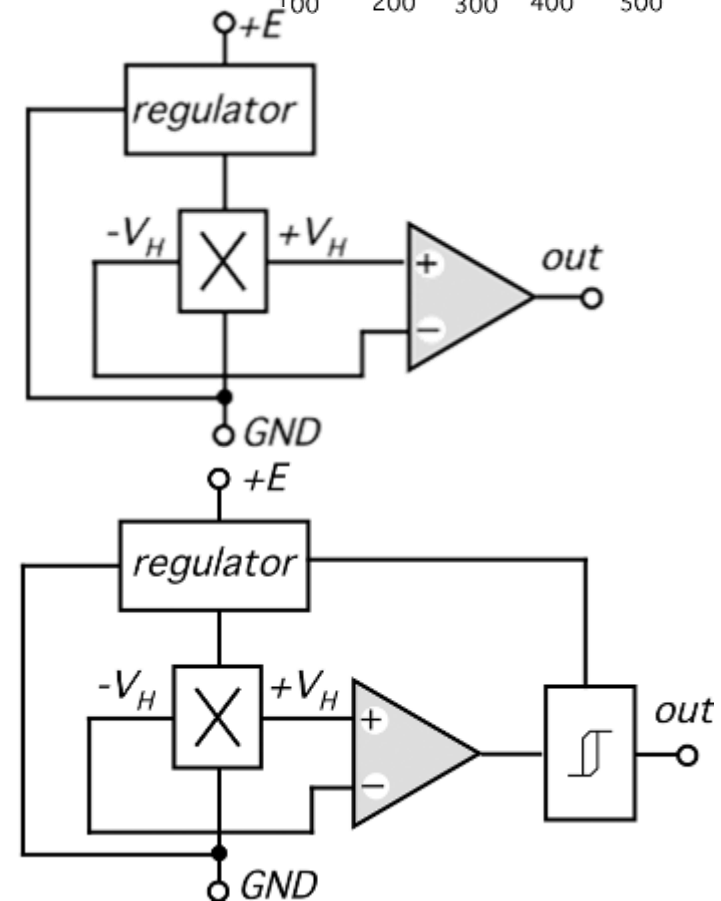
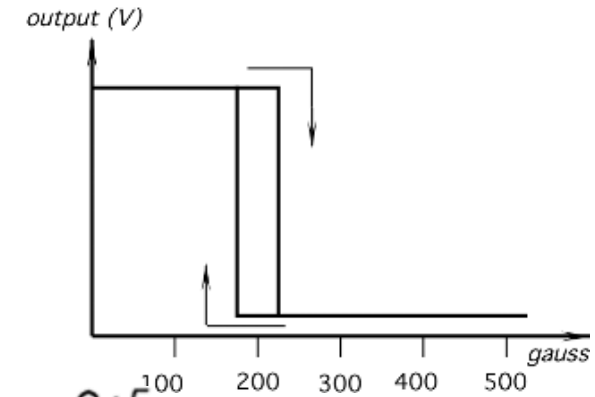
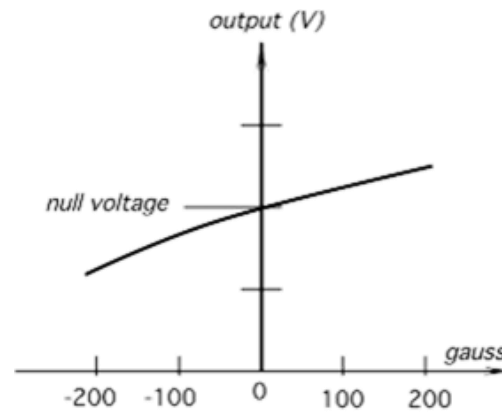
| | |
|---------------------------------------|-----------------------|
| Control current | 3 mA |
| Control resistance, R_I | 2.2 k Ω |
| Control resistance versus temperature | +0.8%/°C |
| Differential output resistance, R_O | 4.4 k Ω |
| Output offset voltage | 5.0 mV (at $B = 0$ G) |
| Sensitivity | 60 μ V/G |
| Sensitivity versus temperature | +0.1%/°C |
| Overall sensitivity | 20 V/ Ω kG |
| Maximum magnetic flux density, B | Unlimited |

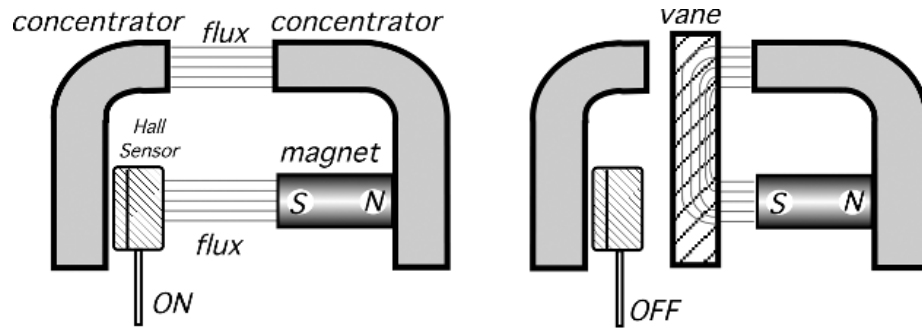
- Hall coefficient (sensitivity) is small (60 μ V/Gauss)
 - most sensed fields are smaller than 1×10^4 G
 - Hall voltage can be as small as a few μ V
 - Hall voltage must often be amplified before processing
- sensitivity and resistance are temperature dependent
 - same polarity for both effects in semiconductor
 - different polarities in metals (allows compensation)

- two types of sensors
 - linear sensor
 - threshold sensor

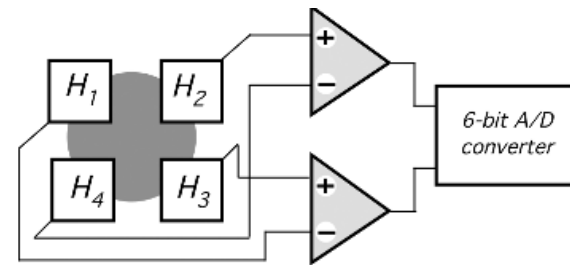
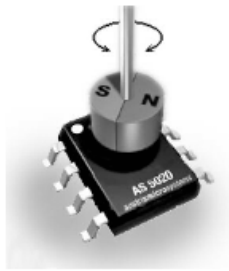
- linear sensor
 - basic hall effect sensor
 - voltage regulator to create constant control current
 - amplifier to enlarge Hall voltage (why an offset voltage?)

- threshold sensor
 - linear sensor
 - Schmitt trigger with build-in hysteresis





threshold sensor



linear (rotation) sensor

